Descriptive Statistics and Probability Test Review

1. The following frequency distribution of marks has mean 4.5.

The following table gives the examination grades for 120 students.

Mark	1	2	3	4	5	6	7
Frequency	2	4	6	9	x	9	4

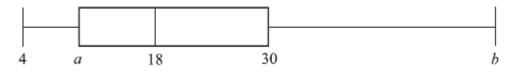
(a) Find the value of *x*.

2.

(b) Write down the standard deviation.

Grade	Number of students	Cumulative frequency
1	9	9
2	25	34
3	35	р
4	q	109
5	11	120

- (a) Find the value of p & q.
- (b) Find the mean grade.
- (c) Write down the standard deviation.
- **3.** The following diagram is a box and whisker plot for a set of data.



The interquartile range is 20 and the range is 40.

- (a) Write down the median value.
- (b) Find the value of a & b.

(4) (Total 5 marks)

1

Test on May 4/5

(4)

(2) (Total 6 marks)

(4)

(2)

(1) (Total 7 marks)

(1)

4. A standard die is rolled 36 times. The results are shown in the following table.

Score	1	2	3	4	5	6
Frequency	3	5	4	6	10	8

- (a) Write down the standard deviation.
- (b) Write down the median score.
- (c) Find the interquartile range.

(1)

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(3)
(Total 6 marks)
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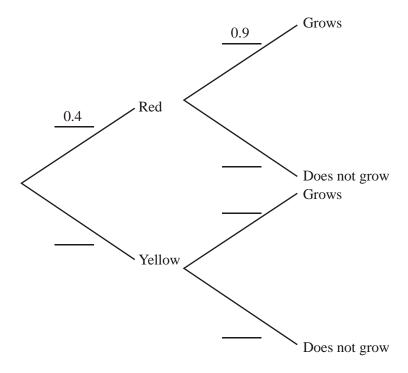
- 5. The following is a cumulative frequency diagram for the time *t*, in minutes, taken by 80 students to complete a task.
 - 80 Write down the median. (a) (1) 70 Find the interquartile range. (b) (3) 60 cumulative frequency 50 40 30 20 10 0 10 20 30 40 50 time (t) Complete the frequency table below. (c)

Time (minutes)	Number of students
$0 \le t < 10$	5
$10 \le t < 20$	
$20 \le t < 30$	20
$30 \le t < 40$	24
$40 \le t < 50$	
$50 \le t < 60$	6

60

(2)

- 6. A packet of seeds contains 40% red seeds and 60% yellow seeds. The probability that a red seed grows is 0.9, and that a yellow seed grows is 0.8. A seed is chosen at random from the packet.
 - (a) Complete the probability tree diagram below.



(3)

(3)

(7)

(b) (i) Calculate the probability that the chosen seed is red and grows.

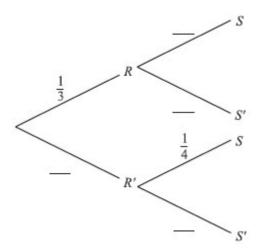
- (ii) Calculate the probability that the chosen seed grows.
- (iii) Given that the seed grows, calculate the probability that it is red.

(7) (Total 10 marks)

7. The following probabilities were found for two events *R* and *S*.

$$P(R) = \frac{1}{3}, P(S | R) = \frac{4}{5}, P(S | R') = \frac{1}{4}.$$

(a) **Copy** and **complete** the tree diagram.



(b) Find the following probabilities.

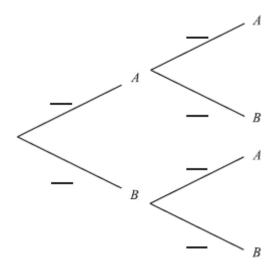
(i) $P(R \cap S)$.

- (ii) P(S).
- (iii) $P(R \mid S)$.

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(Total 10 marks)

- 8. A bag contains four apples (*A*) and six bananas (*B*). A fruit is taken from the bag and eaten. Then a second fruit is taken and eaten.
 - (a) Complete the tree diagram below by writing probabilities in the spaces provided.



(3)

(b) Find the probability that one of each type of fruit was eaten.

(3) (Total 6 marks)

9. The eye colour of 97 students is recorded in the chart below.

	Brown	Blue	Green
Male	21	16	9
Female	19	19	13

One student is selected at random.

- (a) Write down the probability that the student is a male.
- (b) Write down the probability that the student has green eyes, given that the student is a female.
- (c) Find the probability that the student has green eyes or is male.

(Total 6 marks)

(1)

(4)

- 10. Let *A* and *B* be independent events, where P(A) = 0.6 and P(B) = x.
 - (a) Write down an expression for $P(A \cap B)$.
 - (b) Given that $P(A \cup B) = 0.8$,
 - (i) find x;
 - (ii) find $P(A \cap B)$.
 - (c) **Hence**, explain why *A* and *B* are **not** mutually exclusive.

11. Consider the independent events *A* and *B*. Given that P(B) = 2P(A), and $P(A \cup B) = 0.52$, find P(B).

(Total 7 marks)

12. In any given season, a soccer team plays 65 % of their games at home. When the team plays at home, they win 83 % of their games. When they play away from home, they win 26 % of their games.

The team plays one game.

- (a) Find the probability that the team wins the game.
- (b) If the team does not win the game, find the probability that the game was played at home.

(4) (Total 8 marks)

(4)

13. The number of hours of sleep of 21 students are shown in the frequency table below.

Hours of sleep	Number of students
4	2
5	5
6	4
7	3
8	4
10	2
12	1

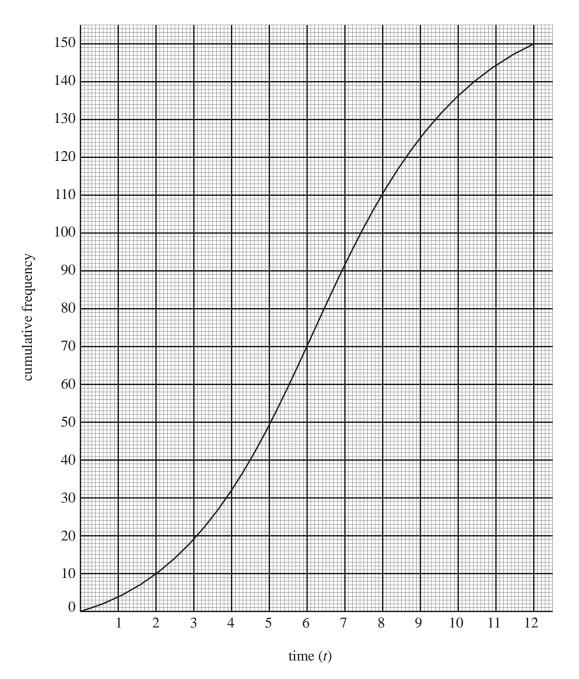
Find

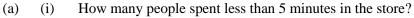
(a) the median;

- (b) the lower quartile;
- (c) the interquartile range.

(Total 6 marks)

14. The following is the cumulative frequency curve for the time, *t* minutes, spent by 150 people in a store on a particular day.





(ii) Find the number of people who spent between 5 and 7 minutes in the store.

- (iii) Find the median time spent in the store.
- (b) Given that 40% of the people spent longer than k minutes, find the value of k.

(6)

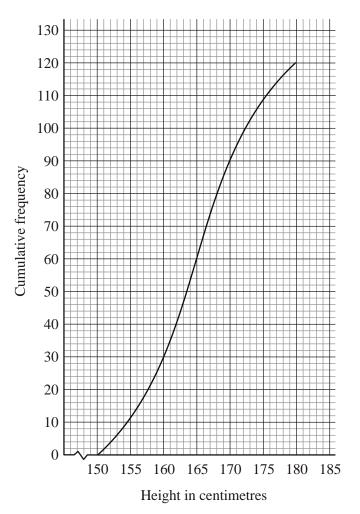
(3)

(c) (i) **On your answer sheet**, copy and complete the following frequency table.

t (minutes)	$0 \le t < 2$	$2 \le t < 4$	$4 \le t < 6$	$6 \le t < 8$	$8 \le t < 10$	$10 \le t < 12$
Frequency	10	23				15

(ii) Hence, calculate an estimate for the mean time spent in the store.

15. The cumulative frequency graph below shows the heights of 120 girls in a school.



- (a) Using the graph
 - (i) write down the median;
 - (ii) find the interquartile range.
- (b) Given that 60% of the girls are taller than a cm, find the value of a.

(Total 6 marks)

16. A company uses two machines, A and B, to make boxes. Machine A makes 60 % of the boxes.

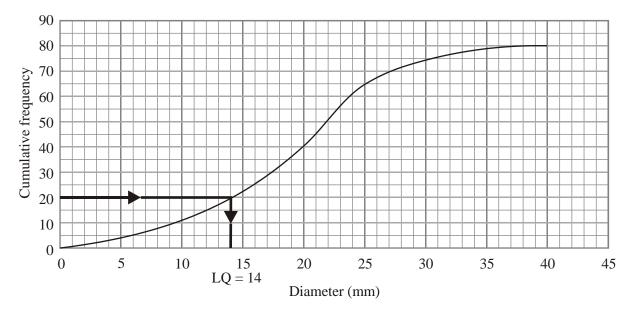
80 % of the boxes made by machine A pass inspection. 90 % of the boxes made by machine B pass inspection.

A box is selected at random.

- (a) Find the probability that it passes inspection.
- (b) The company would like the probability that a box passes inspection to be 0.87. Find the percentage of boxes that should be made by machine B to achieve this.

(3)

17. A student measured the diameters of 80 snail shells. His results are shown in the following cumulative frequency graph. The lower quartile (LQ) is 14 mm and is marked clearly on the graph.



(a) On the graph, mark clearly in the same way and write down the value of

- (i) the median;
- (ii) the upper quartile.
- (b) Write down the interquartile range.
- (c) Find the smallest diameter of the upper 10% of the snails.

(Total 8 marks)