

1. evidence of substituting into binomial expansion (M1)

$$e.g. a^5 + \binom{5}{1}a^4b + \binom{5}{2}a^3b^2 + \dots$$

identifying correct term for  $x^4$

evidence of calculating the factors, in any order

(M1)  
A1A1A1

$$e.g. \binom{5}{2}, 27x^6, \frac{4}{x^2}; 10(3x^2)^3\left(\frac{-2}{x}\right)^2$$

*Note: Award A1 for each correct factor.*

$$\text{term} = 1080x^4$$

A1 N2

*Note: Award M1M1A1A1A1A0 for 1080 with working shown.*

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2. (a) 7 terms A1 N1

- (b) A valid approach (M1)

Correct term **chosen**  $\binom{6}{3}(x^3)^3(-3x)^3$  A1

Calculating  $\binom{6}{3} = 20, (-3)^3 = -27$  (A1)(A1)

Term is  $-540x^{12}$  A1 N3

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3. The constant term will be the term independent of the variable  $x$ . (R1)

$$\left(x - \frac{2}{x^2}\right)^9 = x^9 + 9x^8\left(\frac{-2}{x^2}\right) + \dots + \binom{9}{3}x^6\left(\frac{-2}{x^2}\right)^3 + \dots + \left(\frac{-2}{x^2}\right)^9$$
 (M1)

$$\binom{9}{3}x^6\left(\frac{-2}{x^2}\right)^3 = 84x^6\left(\frac{-8}{x^6}\right)$$
 (A1)

$$= -672$$
 (A1)

[4]

4. (a) correct equation in the form  $r = a + tb$  A2 N2 2

$$r = \begin{pmatrix} 1 \\ -1 \\ 2 \end{pmatrix} + t \begin{pmatrix} 1 \\ 3 \\ -2 \end{pmatrix}$$

(b) (i) attempt to substitute  $t = 2$  into the equation (M1)

$$e.g. \begin{pmatrix} 2 \\ 6 \\ -4 \end{pmatrix}, \begin{pmatrix} 1 \\ -1 \\ 2 \end{pmatrix} + 2 \begin{pmatrix} 1 \\ 3 \\ -2 \end{pmatrix}$$

$$\overrightarrow{OP} = \begin{pmatrix} 3 \\ 5 \\ -2 \end{pmatrix} 3$$

A1 N2

(ii) correct substitution into formula for magnitude A1

$$e.g. \sqrt{3^2 + 5^2 + (-2)^2}, \sqrt{3^2 + 5^2 + 2^2}$$

$$|\overrightarrow{OP}| = \sqrt{38}$$

A1 N1 4

[6]

5. (a)  $\overrightarrow{OB} = \begin{pmatrix} 10 \\ 5 \end{pmatrix}$  (A1) (C1)

$$\overrightarrow{AC} = \begin{pmatrix} -3 \\ 6 \end{pmatrix} \quad (A1) (C1)$$

(b)  $\overrightarrow{OB} \cdot \overrightarrow{AC} = (10 \times (-3)) + (5 \times 6) = 0$  (M1)  
Angle =  $90^\circ$  (A1) (C2)

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6. Angle between lines = angle between direction vectors. (M1)

Direction vectors are  $\begin{pmatrix} 4 \\ 3 \end{pmatrix}$  and  $\begin{pmatrix} 1 \\ -1 \end{pmatrix}$ . (A1)

$$\begin{pmatrix} 4 \\ 3 \end{pmatrix} \cdot \begin{pmatrix} 1 \\ -1 \end{pmatrix} = \left| \begin{pmatrix} 4 \\ 3 \end{pmatrix} \right| \left| \begin{pmatrix} 1 \\ -1 \end{pmatrix} \right| \cos \theta \quad (M1)$$

$$4(1) + 3(-1) = (\sqrt{4^2 + 3^2})(\sqrt{1^2 + (-1)^2}) \cos \theta \quad (A1)$$

$$\cos \theta = \frac{1}{5\sqrt{2}} = 0.1414 \quad (A1)$$

$$\theta = 81.9^\circ \text{ (3 sf), (1.43 radians)} \quad (A1) (C6)$$

**Note:** If candidates find the angle between the vectors

$\begin{pmatrix} 4 \\ -1 \end{pmatrix}$  and  $\begin{pmatrix} 2 \\ 4 \end{pmatrix}$ , award marks as below:

Angle required is between  $\begin{pmatrix} 4 \\ -1 \end{pmatrix}$  and  $\begin{pmatrix} 2 \\ 4 \end{pmatrix}$  (M0)(A0)

$$\begin{pmatrix} 4 \\ -1 \end{pmatrix} \cdot \begin{pmatrix} 2 \\ 4 \end{pmatrix} = \left| \begin{pmatrix} 4 \\ -1 \end{pmatrix} \right| \left| \begin{pmatrix} 2 \\ 4 \end{pmatrix} \right| \cos \theta \quad (\text{M1})$$

$$4(2) + (-1)4 = \left( \sqrt{4^2 + (-1)^2} \right) \left( \sqrt{2^2 + 4^2} \right) \cos \theta \quad (\text{A1})$$

$$\frac{4}{\sqrt{17}\sqrt{20}} = \cos \theta = 0.2169 \quad (\text{A1})$$

$$\theta = 77.5^\circ \text{ (3sf), (1.35 radians)} \quad (\text{A1}) \quad (\text{C4})$$

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7. (a) evidence of appropriate approach (M1)

$$e.g. \vec{BC} = \vec{BA} + \vec{AC}, \begin{pmatrix} -2 \\ -3 \\ 2 \end{pmatrix} = \begin{pmatrix} 6 \\ -2 \\ 3 \end{pmatrix}$$

$$\vec{BC} = \begin{pmatrix} -8 \\ -1 \\ -1 \end{pmatrix}$$

A1 N2

(b) attempt to find the length of  $\vec{AB}$  (M1)

$$|\vec{AB}| = \sqrt{6^2 + (-2)^2 + 3^2} \quad (= \sqrt{36 + 4 + 9} = \sqrt{49} = 7) \quad (\text{A1})$$

$$\text{unit vector is } \frac{1}{7} \begin{pmatrix} 6 \\ -2 \\ 3 \end{pmatrix} = \begin{pmatrix} \frac{6}{7} \\ -\frac{2}{7} \\ \frac{3}{7} \end{pmatrix}$$

A1 N2

- (c) recognizing that the dot product or  $\cos \theta$  being 0 implies perpendicular (M1)  
 correct substitution in a scalar product formula A1

$$e.g. (6) \times (-2) + (-2) \times (-3) + (3) \times (2), \cos \theta = \frac{-12 + 6 + 6}{7 \times \sqrt{17}}$$

correct calculation A1

$$e.g. \vec{AB} \bullet \vec{AC} = 0, \cos \theta = 0$$

therefore, they are perpendicular AG N0

[8]

8. evidence of appropriate approach (M1)

$$e.g. \begin{pmatrix} 2 \\ 3 \\ -1 \end{pmatrix} + s \begin{pmatrix} 5 \\ -3 \\ 2 \end{pmatrix} = \begin{pmatrix} 9 \\ 2 \\ 2 \end{pmatrix} + t \begin{pmatrix} -3 \\ 5 \\ -1 \end{pmatrix}$$

two correct equations A1A1

$$e.g. 2 + 5s = 9 - 3t, 3 - 3s = 2 + 5t, -1 + 2s = 2 - t$$

attempting to solve the equations (M1)

one correct parameter  $s = 2, t = -1$  A1

P is  $(12, -3, 3)$   $\left( \begin{matrix} \text{accept} \\ \begin{pmatrix} 12 \\ -3 \\ 3 \end{pmatrix} \end{matrix} \right)$  A1 N3

[6]

9. (a)  $\begin{pmatrix} 2x \\ x-3 \end{pmatrix} \bullet \begin{pmatrix} x+1 \\ 5 \end{pmatrix} = 0$  (M1)(M1)

$$\Rightarrow 2x(x+1) + (x-3)(5) = 0$$
 (A1)

$$\Rightarrow 2x^2 + 7x - 15 = 0$$
 (C3)

(b) **METHOD 1**

$$2x^2 + 7x - 15 = (2x - 3)(x + 5) = 0$$

$$\Rightarrow x = \frac{3}{2} \text{ or } x = -5$$

(A1) (C1)

**METHOD 2**

$$x = \frac{-7 \pm \sqrt{7^2 - 4(2)(-15)}}{2(2)}$$

$$\Rightarrow x = \frac{3}{2} \text{ or } x = -5$$

(A1) (C1)

[4]